

Determination of Reaction Rate Parameters in Heterogeneous Particulate Systems

Dr. Alvaro A. ESTUPINAN DONOSO

 FACULTY OF SCIENCE, TECHNOLOGY AND MEDICINE



UNIVERSITÉ DU
LUXEMBOURG



UNIVERSITY OF LUXEMBOURG
Department of Physics
and Materials Science



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High Performance Computing in Luxembourg

Where is Luxembourg?

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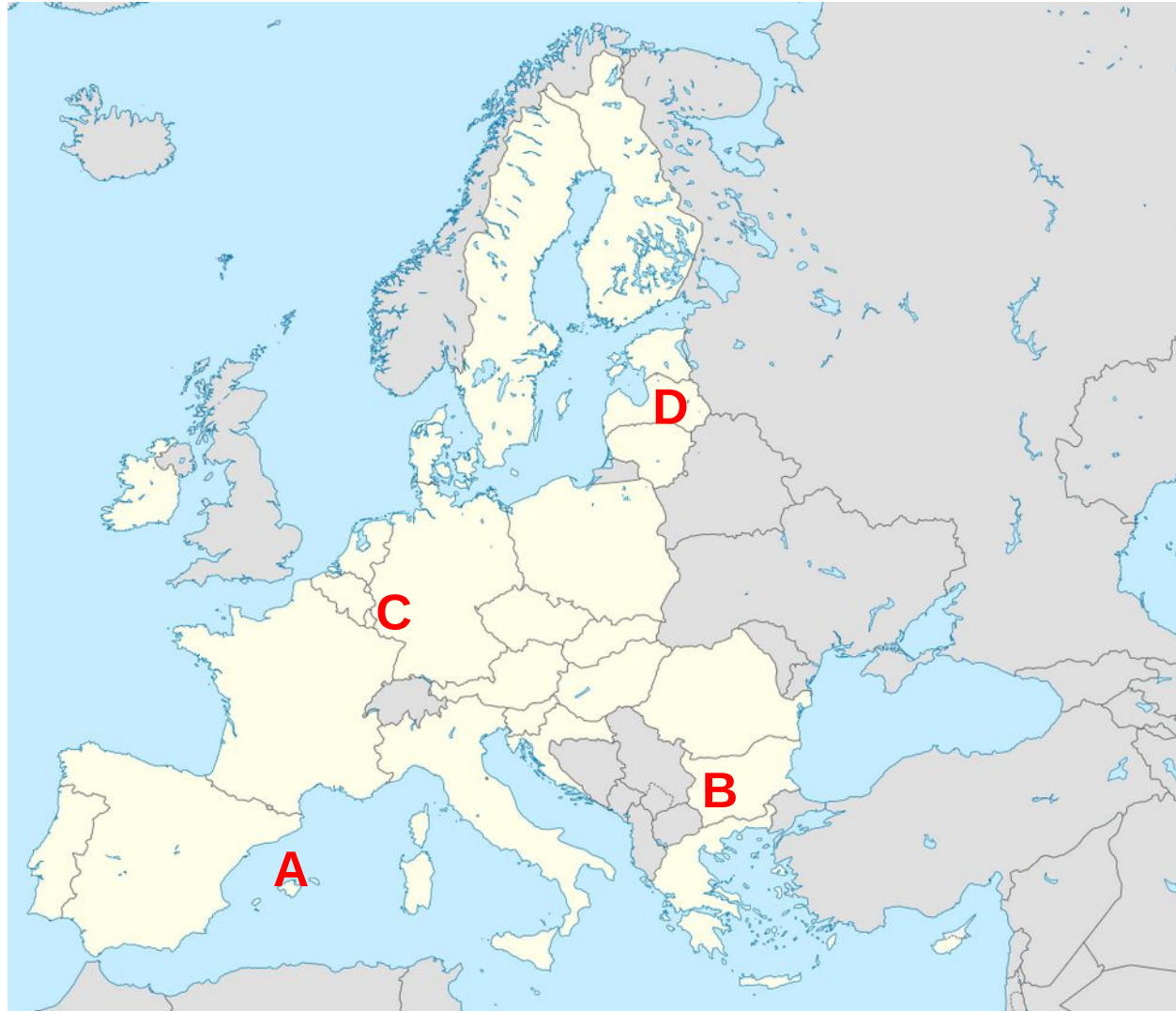
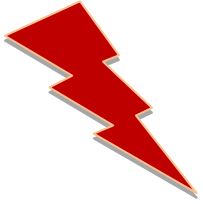


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Where is Luxembourg?

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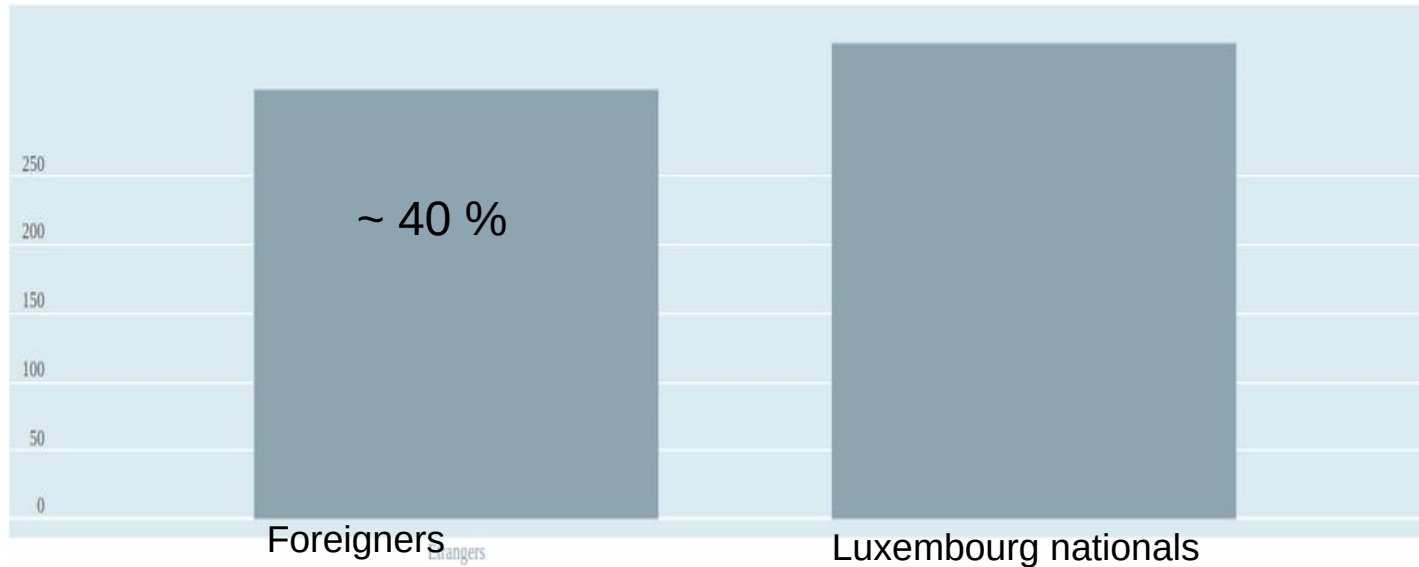


EU map

LUXEMBOURG



Fréquence: Annuelle • Période: 2023



© Population par sexe et par nationalité au 1er janvier (x 1 000) STATEC



Facts & Figures April 2023

THE UNIVERSITY



2003
Foundation

3

Faculties

3

Campuses

3



Interdisciplinary Centres

RANKINGS

#25

in the THE (Times Higher Education) Young University Rankings 2022

among the top
#250

best universities worldwide according to the THE World University Rankings 2023

#4

worldwide for its international outlook according to the THE World University Rankings 2023

PEOPLE

3,000 Bachelor Students

2,400 Staff

2,000 Master Students

300 Professors

1,000 Doctoral candidates

1,500 Academic Staff

14.000+ Alumni (since 2003) thereof 1.500+ doctor's degrees

130 Nationalities

OUR VISION

A University for Luxembourg and the World

OUR MISSION

To be a world-class research university focusing on:

- Cutting-edge Research
- High-quality Education
- Contribution to the social, cultural and economic development of the country

OUR APPROACH

INTERNATIONAL

INTERDISCIPLINARY

MULTILINGUAL

RESEARCH ORIENTED

CLOSE TO EUROPEAN INSTITUTIONS, FINANCIAL INSTITUTIONS AND LEADING INDUSTRY PLAYERS

RESEARCH

2,438

Publications in 2022

1,000+

Ongoing Projects

172

Horizon projects accepted for H2020 and HEU¹

EU funding

22m€

For EU funding awarded in 2022

138

FNR projects accepted in 2022

National funding

44m€

For FNR² funding awarded in 2022



14th International SuperComputing Camp 2023
Cartagena de Indias, Colombia
14-20 May 2023



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UNIVERSITÉ DU
LUXEMBOURG

Who also is behind this contribution?

- **Mónica Arenas**
 - **Maitsetseg Borchuluun**
 - **Léopold Hillah**
 - Dr. Xavier Besseron
 - Dr. Alban Rousset
 - Prof Bernhard Peters
 - Prof Andreas Michels
-
- The HPC cluster of the University of Luxembourg
 - The NanoMag group
 - The LuXDEM research centre
 - Beamline ID16b from the European Synchrotron Radiation Facility (ESRF)
 - Ceratizit Luxembourg sarl

Introduction

- Granular materials
- Reactions in heterogeneous particulate systems
- Numerical representations of reacting particulate systems
 - Lumped, continuous and discrete modeling approaches

Discrete Element Methods (DEM)

- DEM motivation and history
- Thermochemical DEM simulations
 - What simulation parameters are employed in thermochemical DEM simulations
 - A difference between large-scale and small-scale experimentation

Finding kinetic parameters for heterogeneous reaction systems

- A chemical optimization problem
- A grain growth proposed problem

Takeaways

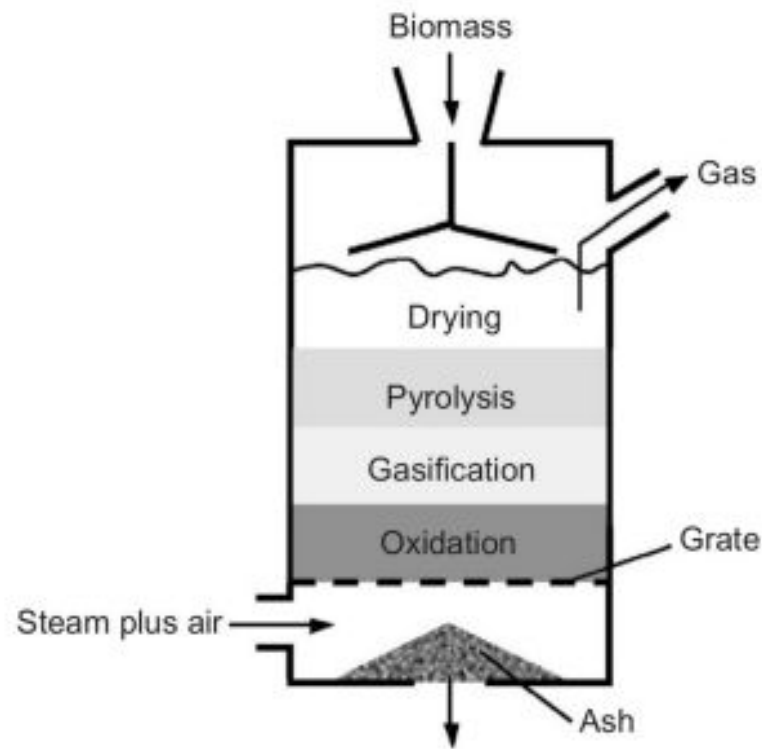
Granular materials

“Granular matter is a system composed of many discrete macroscopic particles”



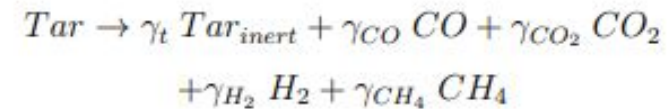
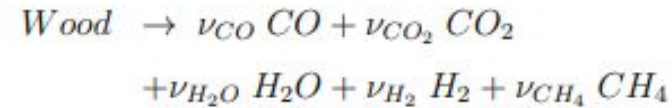
Reactions in heterogeneous particulate systems

Energy from biomass (E.g., Combustion, Gasification)



Biomass Gasifier/Combustor

$$\dot{w}_{H_2O} = \begin{cases} \frac{(T - T_{evap}) \rho c_p}{H_{evap} \delta t} & \text{if } T \geq T_{evap} \\ 0 & \text{if } T \leq T_{evap} \end{cases}$$

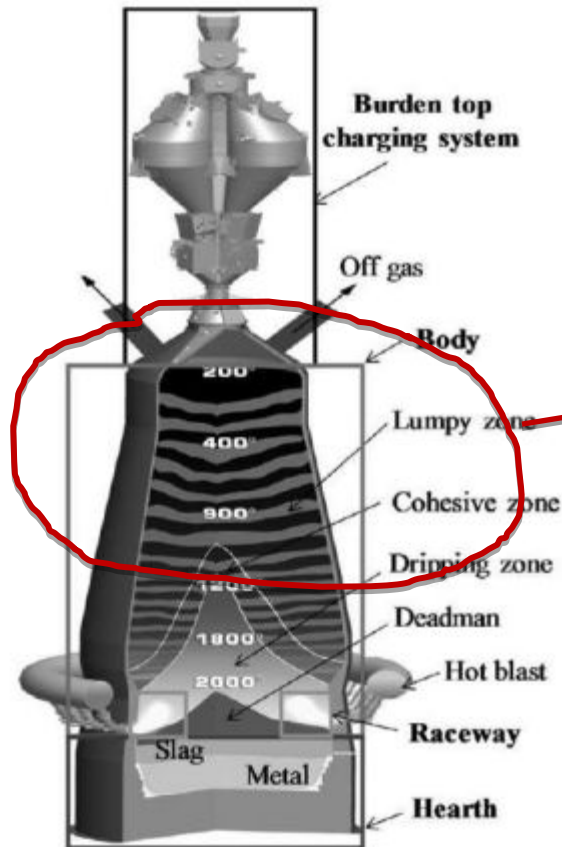


Example of reaction rate model

$$\dot{w}_{wood} = k_0 e^{\frac{-E_a}{RT}} \rho_{wood}$$

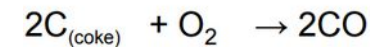
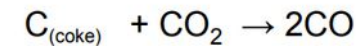
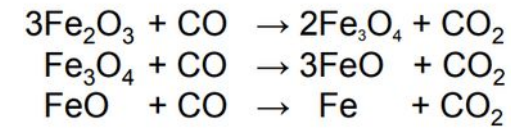
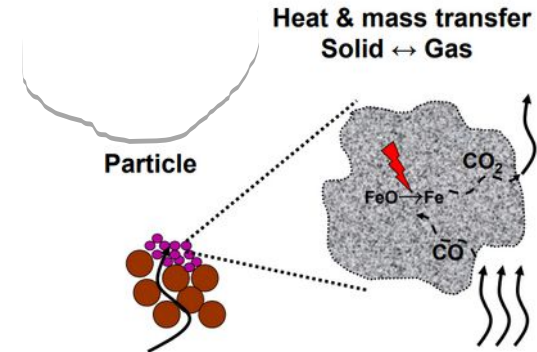
Reactions in heterogeneous particulate systems

Blast furnaces



Blast Furnace

Iron Oxide reduction



Example of reaction rate model

$$\frac{dc_k}{dt} = (\nu_k'' - \nu_k') \cdot k_f(T) \cdot \left(\prod_{i=1}^N c_{R_i}^{\nu_i'} - \frac{1}{K_{\text{eq},c}(T)} \prod_{j=1}^M c_{P_j}^{\nu_j''} \right)$$

Numerical representations of reacting particulate systems

Example of **lumped** model for metal-oxide reduction (WO_3 reduction)

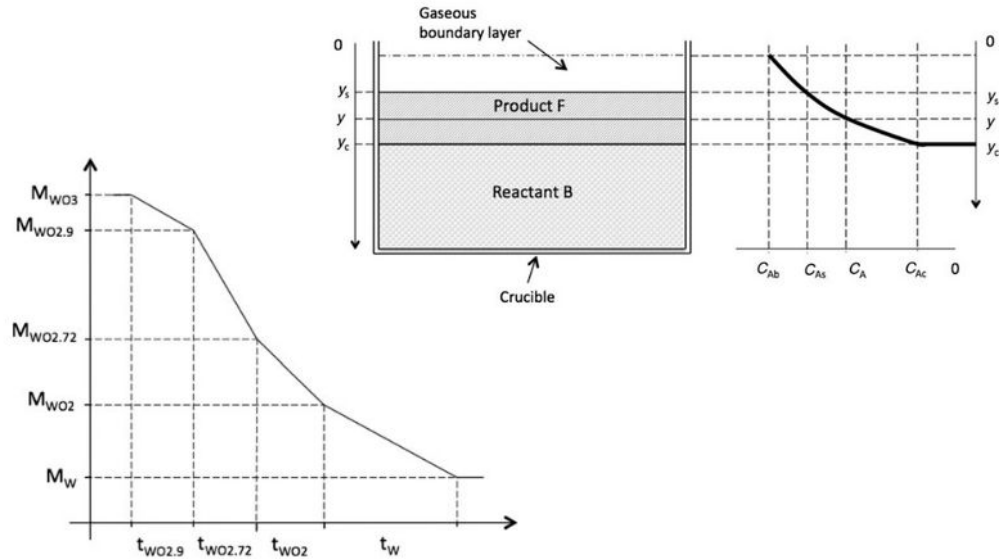


Fig. 18—Reduction scheme for modeling.

$$M_{WO_2} = 0.9310M_0 \quad [21]$$

$$M_W = 0.7930M_0 \quad [22]$$

The different times (min) can be expressed as follows:

$$t_{WO_{2.9}} = \frac{0.69}{3.68002 * P_{H_2}} \quad [23]$$

$$t_{WO_{2.72}} = \frac{M_0 * 0.0124}{22.093 * S_A * P_{H_2}} \quad [24]$$

$$t_{WO_2} = \frac{M_0 * 0.0497}{22.433 * S_A * P_{H_2}} \quad [25]$$

$$t_W = \frac{M_0 * 0.138}{6.5635 * S_A * P_{H_2}} \quad [26]$$

Table 1
Kinetic models and equations

Reaction model	$g(\alpha)$
Diffusion	
One-dimensional	α^2
Two-dimensional	$\alpha + (1 - \alpha)\ln(1 - \alpha)$
Three-dimensional	
Jander equation	$[1 - (1 - \alpha)^{1/3}]^2$
Ginstling-Brounshtein equation	$[1 - (2/3)\alpha] - (1 - \alpha)^{2/3}$
Phase boundary reaction	
Two-dimensional	$1 - (1 - \alpha)^{1/2}$
Three-dimensional	$1 - (1 - \alpha)^{1/3}$
Random nucleation	
First order equation	$-\ln(1 - \alpha)$
Avrami equation	$[-\ln(1 - \alpha)]^{1/2}$
Erofeev equation	$[-\ln(1 - \alpha)]^{1/3}$

Numerical representations of reacting particulate systems

Example of continuous model for heat transfer in packed beds

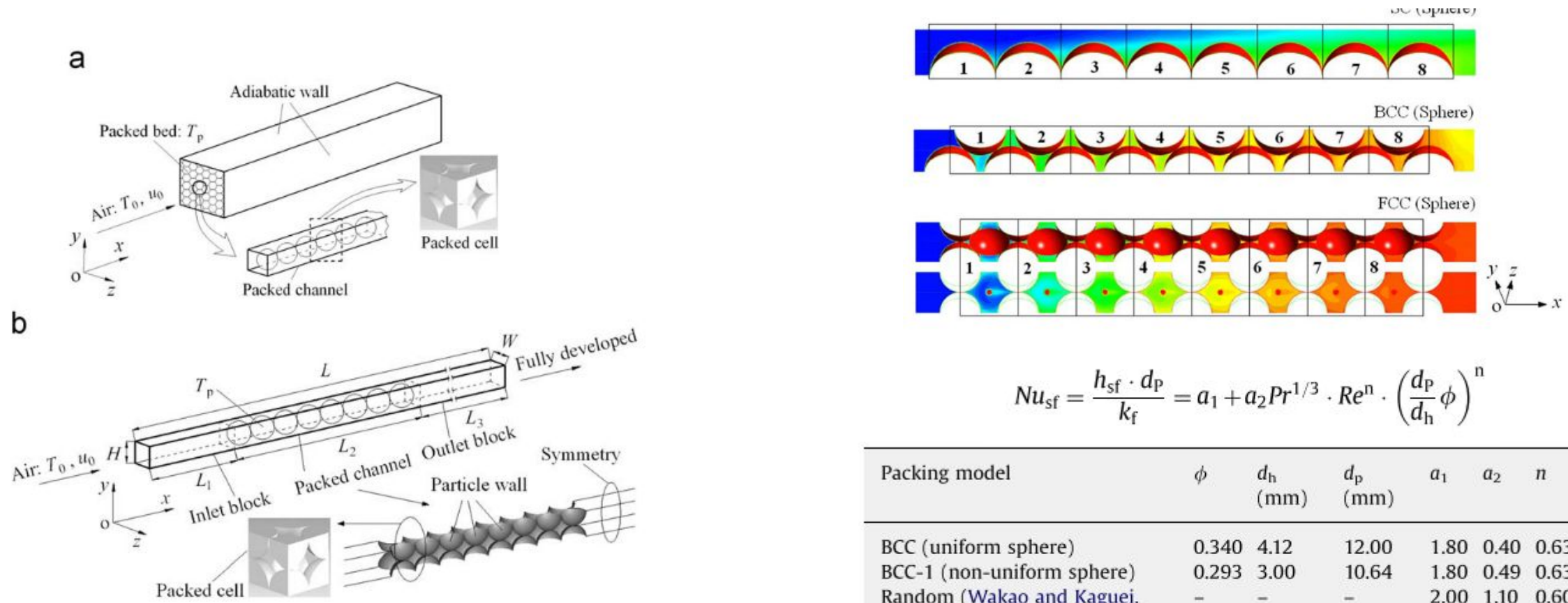


Fig. 1. Physical model: (a) structured packed bed and (b) representative computational domain.

Numerical representations of reacting particulate systems

Example of continuous model for heat transfer in packed beds

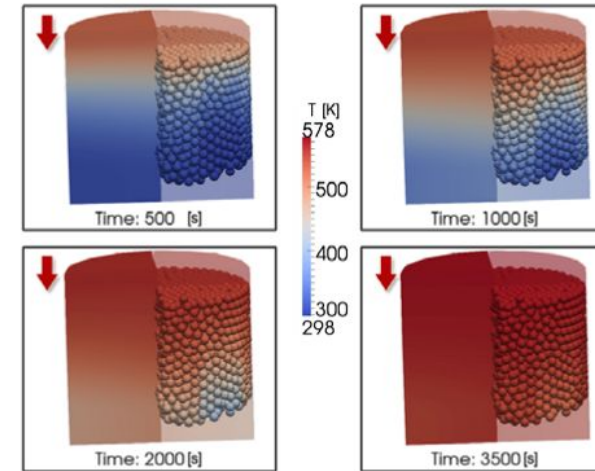
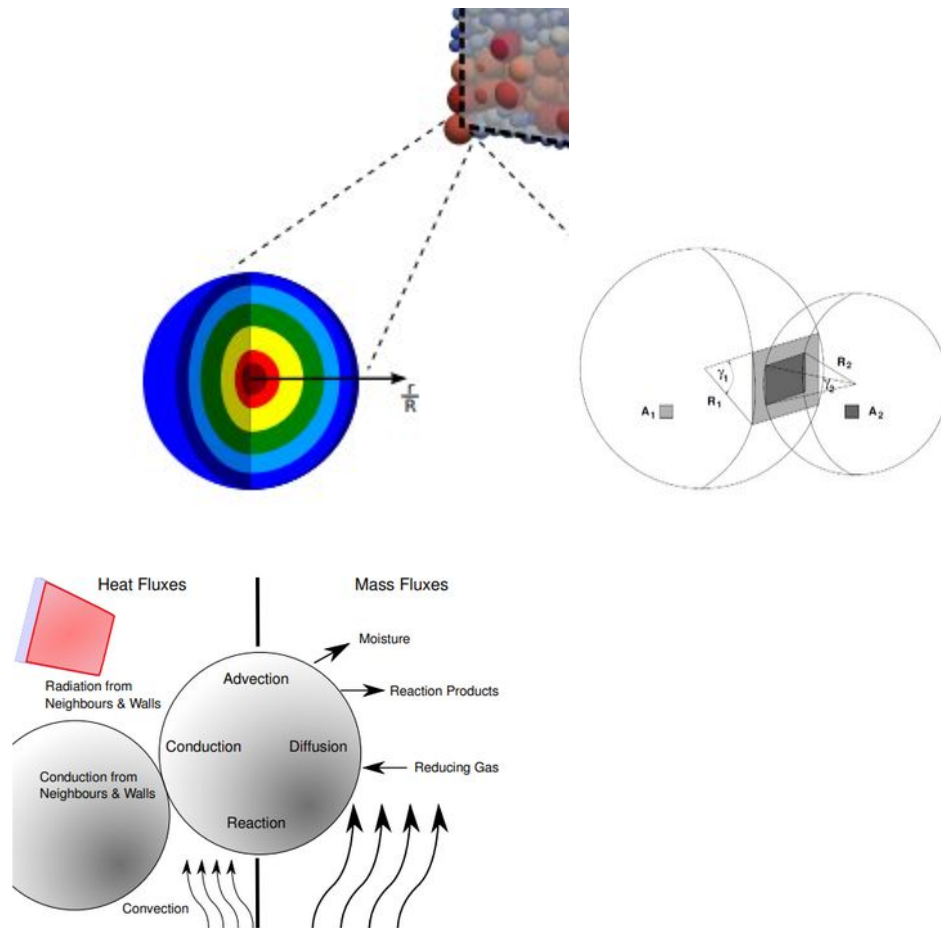


Fig. 8. XDEM fluid and particle temperature predictions at different time steps. Slate, heating-up case.

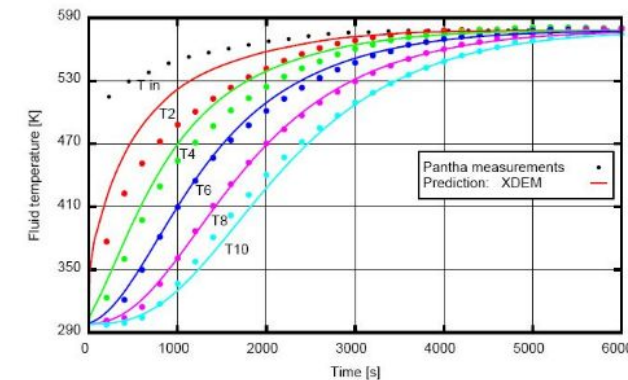
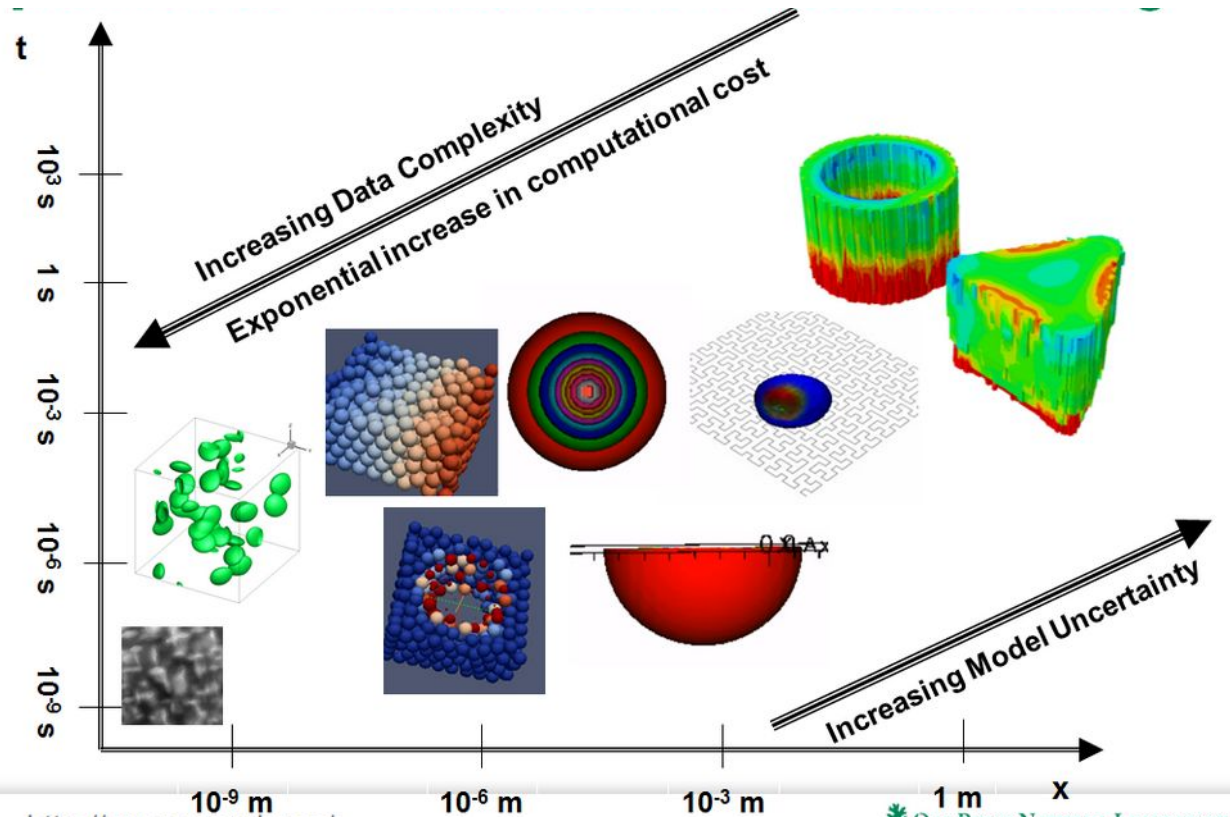


Fig. 9. Comparison between XDEM fluid temperature predictions with the heating-up experiment measurements [27]. Slate, heating-up case

Numerical representations of reacting particulate systems



Increase uncertainty

Lumped modelling

One (or One set) of equations with analytical solution

Continuous modelling

One set of equations (e.g. Navier–Stokes) numerically solved

Discrete modelling

N set of equations (e.g. Navier–Stokes), boundary conditions and sources numerically solved

Continuous + Discrete modelling



Increase computational costs

☐ Introduction

- Granular materials
- Reactions in heterogeneous particulate systems
- Numerical representations of reacting particulate systems
 - Lumped, continuous and discrete modeling approaches

☐ Discrete Element Methods (DEM)

- DEM motivation and history
- Thermochemical DEM simulations

What simulation parameters are employed in thermochemical DEM simulations

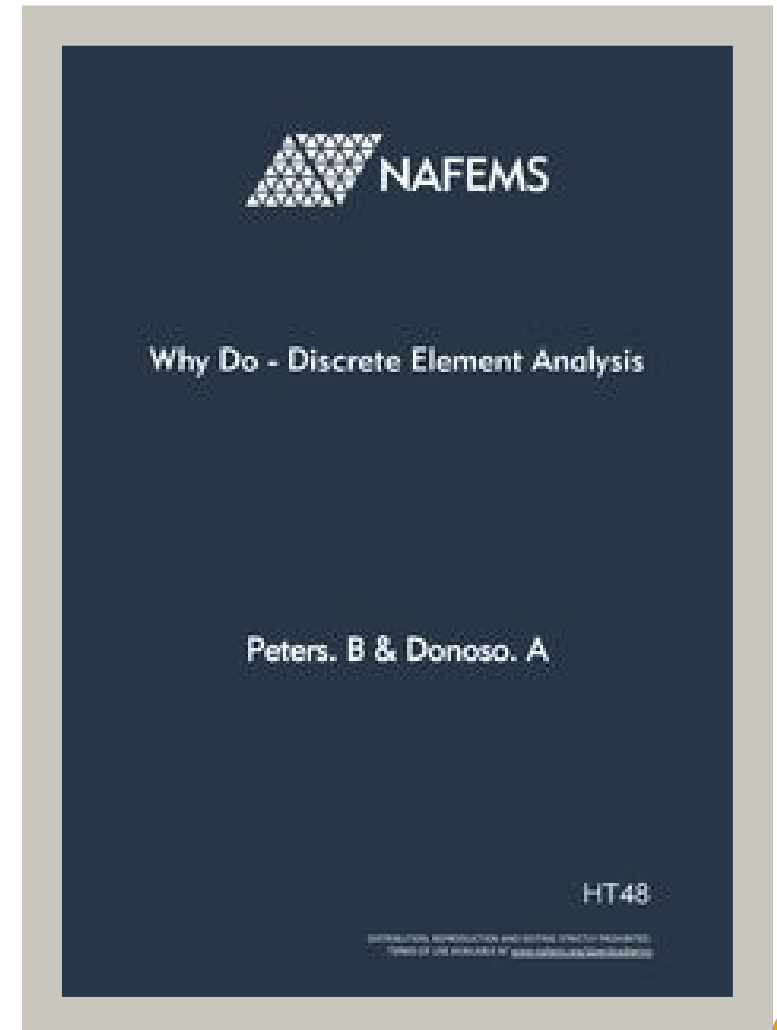
A difference between large-scale and small-scale experimentation

☐ Finding kinetic parameters for heterogeneous reaction systems

- A chemical optimization problem
- A grain growth proposed problem

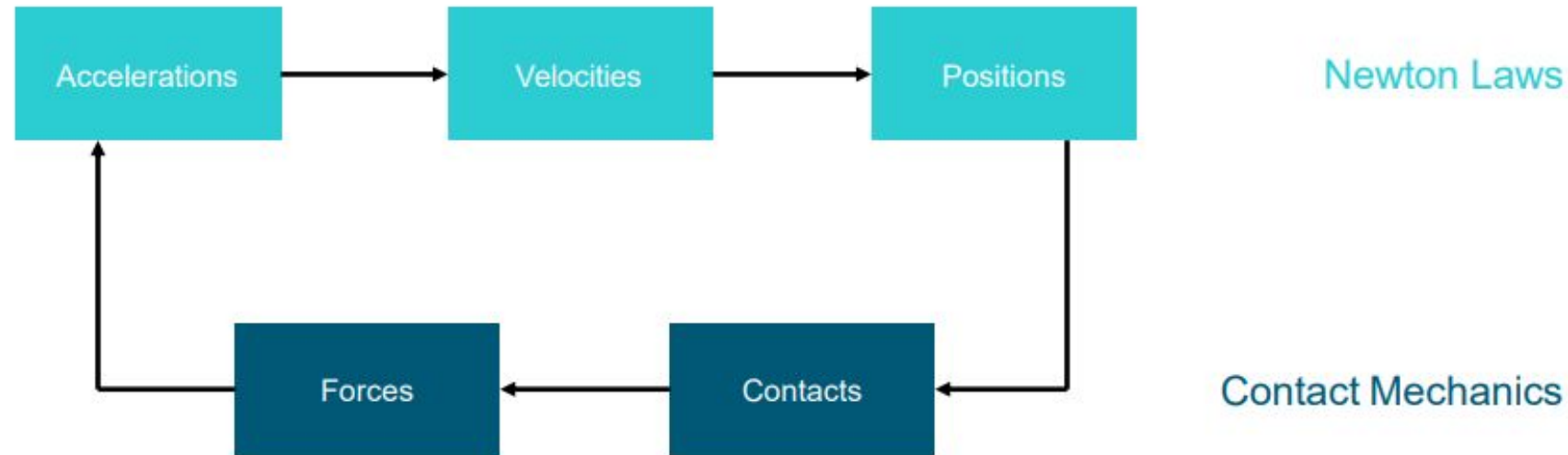
☐ Takeaways

- The Discrete Element Method (DEM) is a discrete approach that **enables accurate numerical calculation of finite particle displacements and rotations**, as well as automated contact detection for a group of particles.
- The method was first **proposed in 1956 by Alder and Wainwright for molecular dynamics studies**. The method was **later developed by Cundall and Strack in the 1970s**, and since then, the principles of the discrete element method, also known as the distinct element method, have been widely used for simulating the behavior of granular materials and other discrete systems.
- Due to its discrete approach, **DEM is particularly well-suited for modeling the bulk behavior of materials**. Its ability to simulate discontinuous media can also **provide valuable insights into various processes, potentially reducing the number of physical experiments required to understand them**.



Discrete Element Method

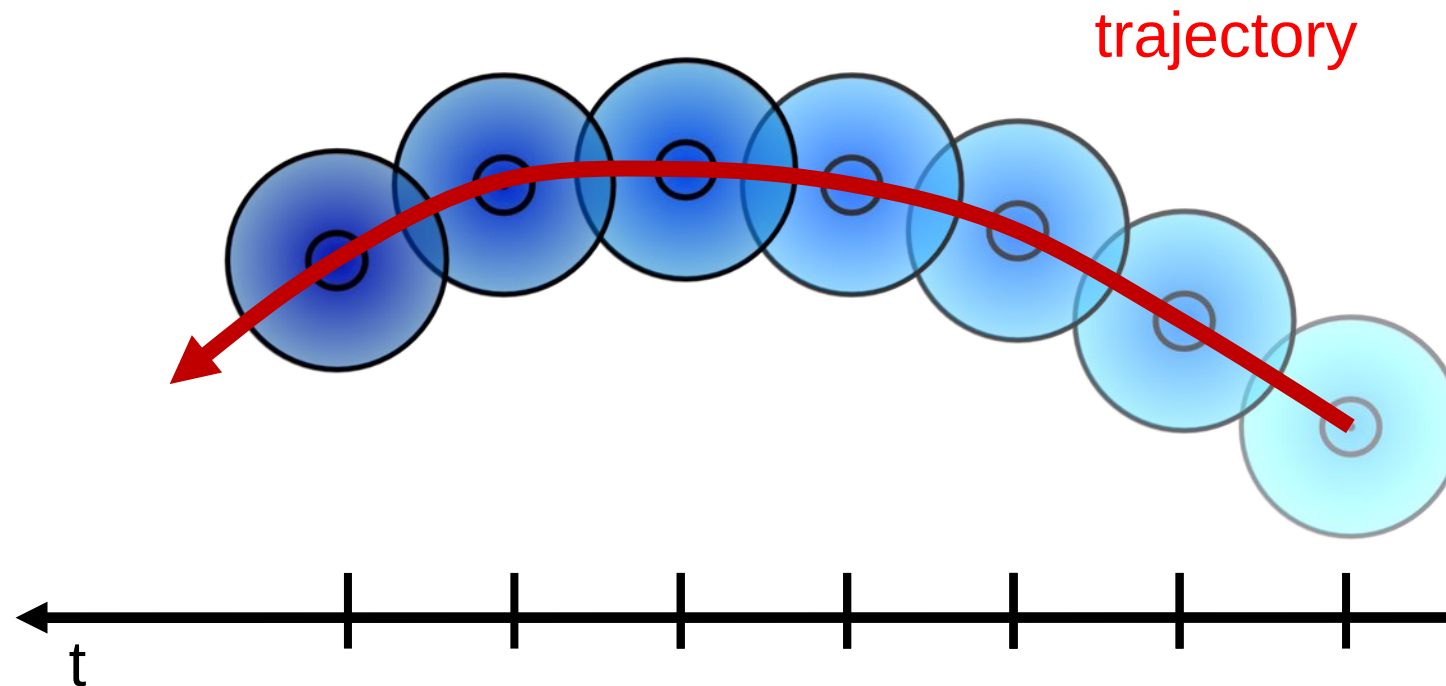
How does it work ?



DEM software utilizes contact detection algorithms and appropriate contact models to calculate the forces acting on particles. By applying Newton's laws of motion and numerical integration, the software can then compute the accelerations, velocities, and positions of the particles.

SRC:  ALTAIR

How can we calculate the trajectory of a particle ?



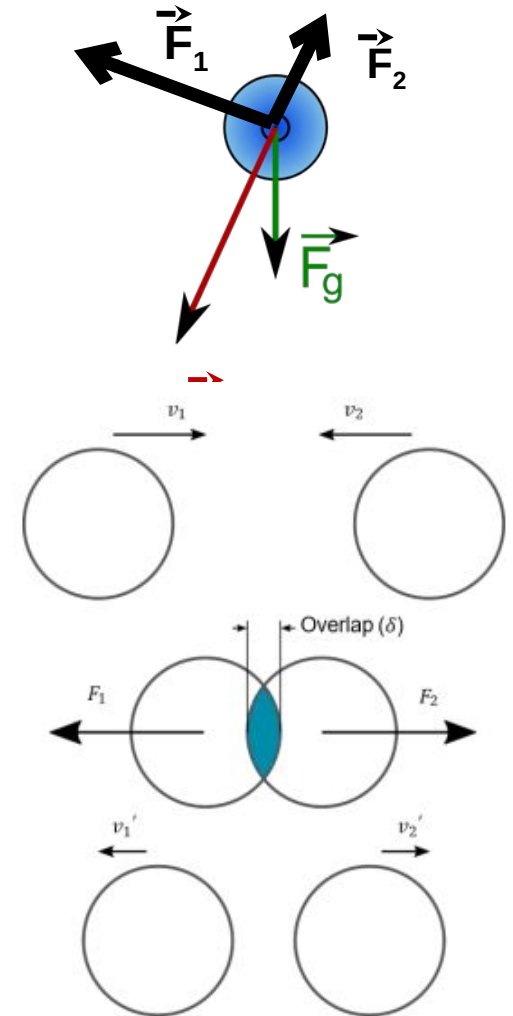
$$\vec{F} = m \cdot \vec{a} \quad \text{Newton's 2nd law of motion}$$

$$\vec{F} = m \cdot \vec{a}(t)$$

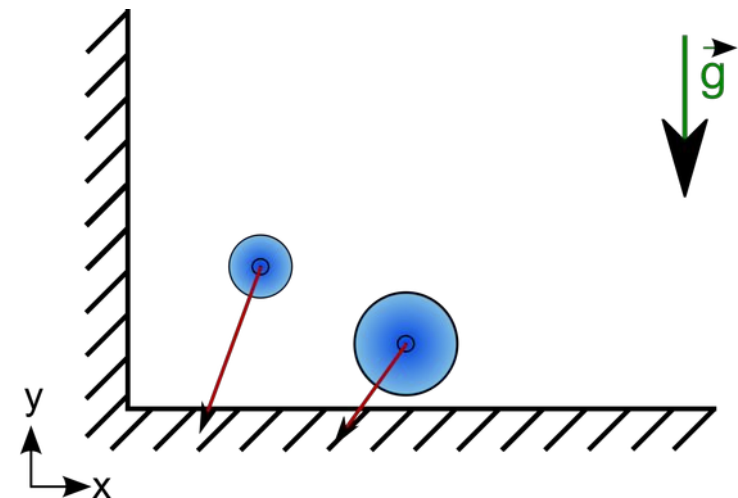
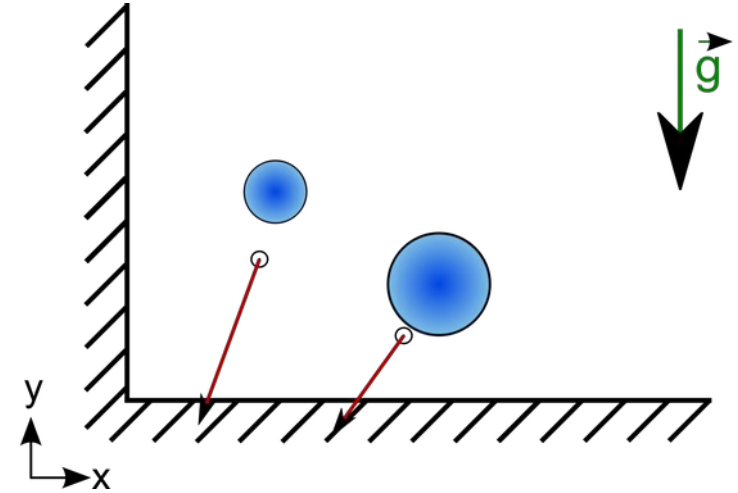
$$\vec{a}(t) = \frac{\sum \vec{F}}{m}$$

$$\int_{t_0}^{t_1} (\dots) dt \rightarrow \vec{x}(t_1) = \vec{v}(t_1) = \vec{v}_0 + \frac{\sum \vec{F}}{m} \cdot (t_1 - t_0)$$

$$\int_{t_0}^{t_1} (\dots) dt \rightarrow \vec{x}(t_1) = \vec{x}_0 + \vec{v}_0 \cdot (t_1 - t_0) + \frac{1}{2} \cdot \frac{\sum \vec{F}}{m} \cdot (t_1 - t_0)^2$$



- Single Particle Contact



Setup

- 2.35M particles
- 10M CFD cells in the fine grid
- 500k CFD cells in the coarse grid
- Co-located partitions + Dual Grid
- Non-uniform distribution

Models for Various Material Behavior

In DEM, different types of material behavior can be simulated by a range of well-established models.

SRC:  ALTAIR



Dry granular material

This type of material can be simulated in DEM by a variety of linear or nonlinear models. The most common ones include Linear Spring or Hertz-Mindlin (no slip), which is a default contact model in EDEM.



Bonding

Particles in DEM can be bonded together to resist tangential and normal movement up to a maximum value (defined by the user) at which the bond breaks. This model is particularly useful in modelling concrete and rock structures.



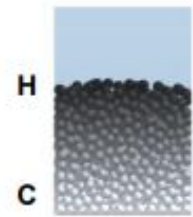
Electrostatics

Longer-range electrostatic interactions can also be modelled in DEM. Particles are assigned a charge and experience forces based on the Coulomb's law. Applications like laser printer behavior can be simulated with such a module.



Cohesion

The cohesion models in DEM can simulate the influence of Van der Waals forces within the contact zones and allow the user to model strongly adhesive systems, such as dry powders or wet materials.



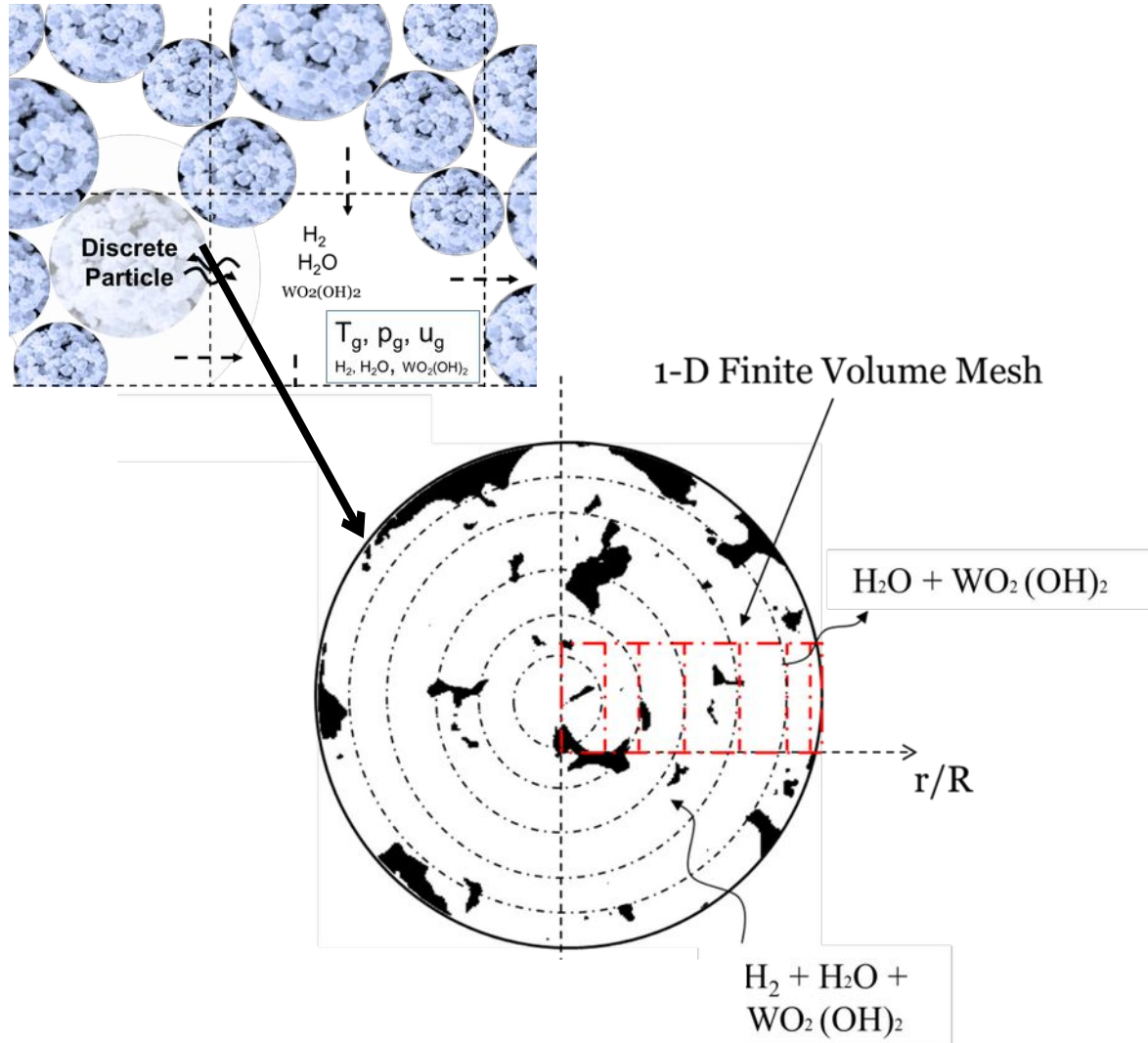
Heat transfer

For dense particulate systems, contacts between particles are substantial and heat conduction can be of significant importance. DEM simulations allow for modelling this inter-particle heat transfer and provide insight into variety of applications ranging from multi-phase reactors to kilns and calciners.

Wikipedia: is a numerical technique that extends the dynamics of granular material or particles as described through the classical discrete element method (DEM) (Cundall [1] and Allen [2]) by additional properties such as the thermodynamic state, stress/strain or electro-magnetic field for each particle. Contrary to a continuum mechanics concept, the XDEM aims at resolving the particulate phase with its various processes attached to the particles. While the discrete element method predicts position and orientation in space and time for each particle, the extended discrete element method additionally estimates properties such as internal temperature and/or species distribution or mechanical impact with structures.

Thermochemical DEM simulations

The eXtended Discrete Element Method (XDEM)



Inner-particle processes predictions by PDEs for conservation:

Mass $\langle \rho_g \rangle^g = \sum_i \langle \rho_{i,g} \rangle^g$

Gas Species g

$$\frac{\partial(\epsilon_p \langle \rho_{i,g} \rangle^g)}{\partial t} + \frac{1}{r^n} \frac{\partial}{\partial r} (r^n \langle \rho_{i,g} \rangle^g \langle u_g \rangle) = \frac{1}{r^n} \frac{\partial}{\partial r} (r^n D_{i,p} \frac{\partial}{\partial r} \langle \rho_{i,g} \rangle^g) + \epsilon_p \sum_k \dot{\omega}_{k,i,g}$$

Energy $\frac{\partial \langle \rho c_p T \rangle}{\partial t} = \frac{1}{r^n} \frac{\partial}{\partial r} \left(r^n \lambda_{\text{eff}} \frac{\partial \langle T \rangle}{\partial r} \right) + \sum_{k=1}^I \dot{\omega}_k H_k$

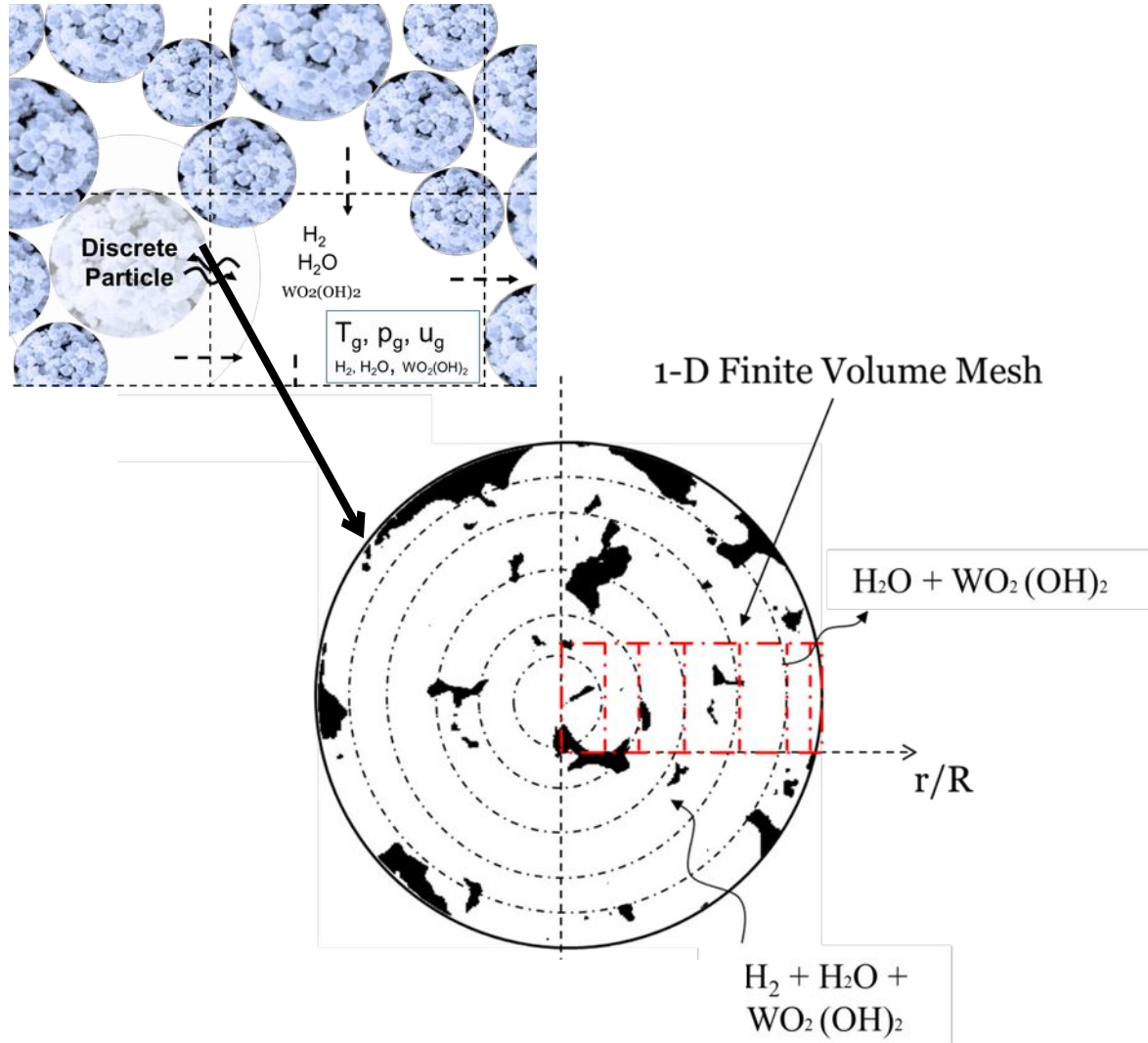
+ Chemical conversion

Solid Species k . E.g., Equilibrium reaction

$$\frac{dc_k}{dt} = k_f(T) \cdot \left(\nu'_k \cdot \prod_{i=1}^N c_{R_i}^{\nu'_i} - \frac{\nu''_k}{K_{\text{eq},c}(T)} \cdot \prod_{j=1}^M c_{P_j}^{\nu''_j} \right)$$

Thermochemical DEM simulations

The eXtended Discrete Element Method (XDEM)



Boundary Conditions and sources

$$\begin{aligned}
 -\lambda_{\text{eff}} \frac{\partial \langle T \rangle}{\partial r} \Big|_{r=0} &= 0 \\
 -\lambda_{\text{eff}} \frac{\partial \langle T \rangle}{\partial r} \Big|_{r=R} &= \alpha(T_R - T_\infty) + \dot{q}_{\text{rad}}'' + \dot{q}_{\text{cond}}'' \\
 -D_{i,\text{eff}} \frac{\partial \langle \rho_i \rangle}{\partial r} \Big|_{r=R} &= \beta_i(\rho_{i,R} - \rho_{i,\infty})
 \end{aligned}$$

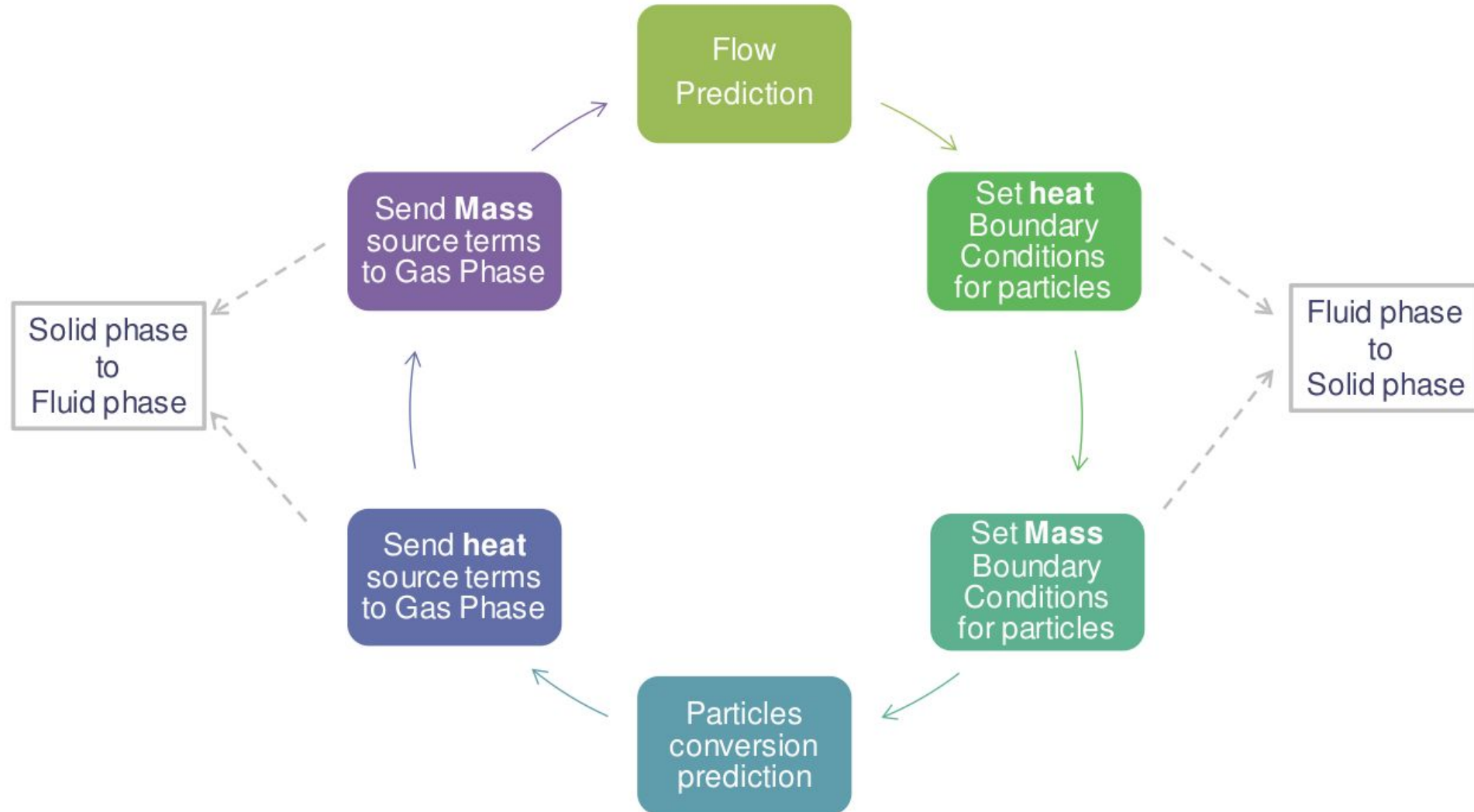
E.g., melting

$$m' = \begin{cases} \frac{(h-h_m)}{h_{sl}\Delta t} & h \geq h_m \\ 0 & h \leq h_m \end{cases}$$

Thermochemical DEM simulations

The eXtended Discrete Element Method (XDEM)

Continuous and discrete phases 4-way coupling for mass and energy



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- Thermochemical DEM simulations

What simulation parameters are employed in thermochemical DEM simulations

A difference between large-scale and small-scale experimentation

☐ Finding kinetic parameters for heterogeneous reaction systems

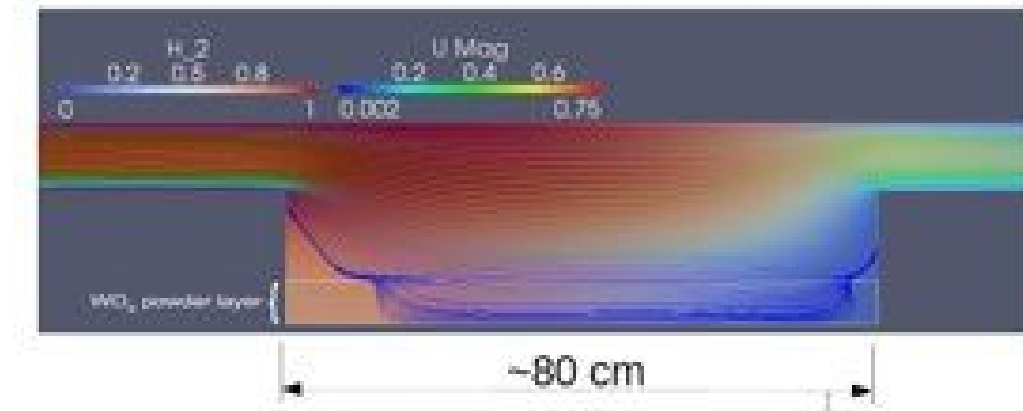
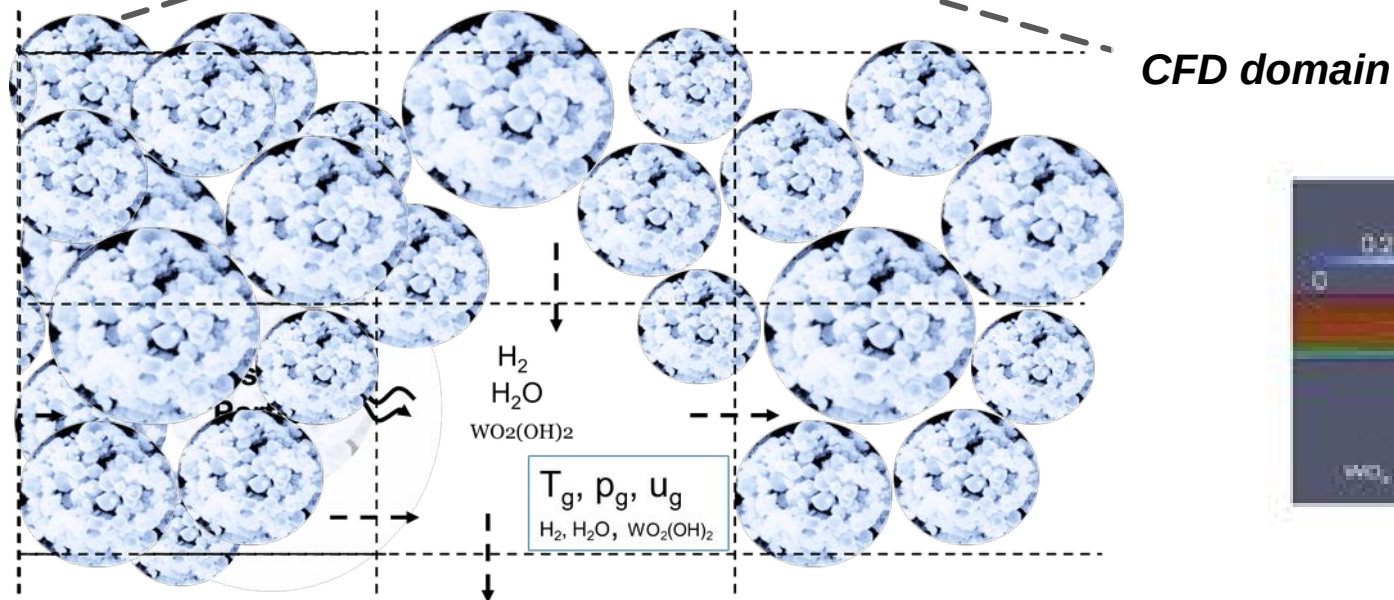
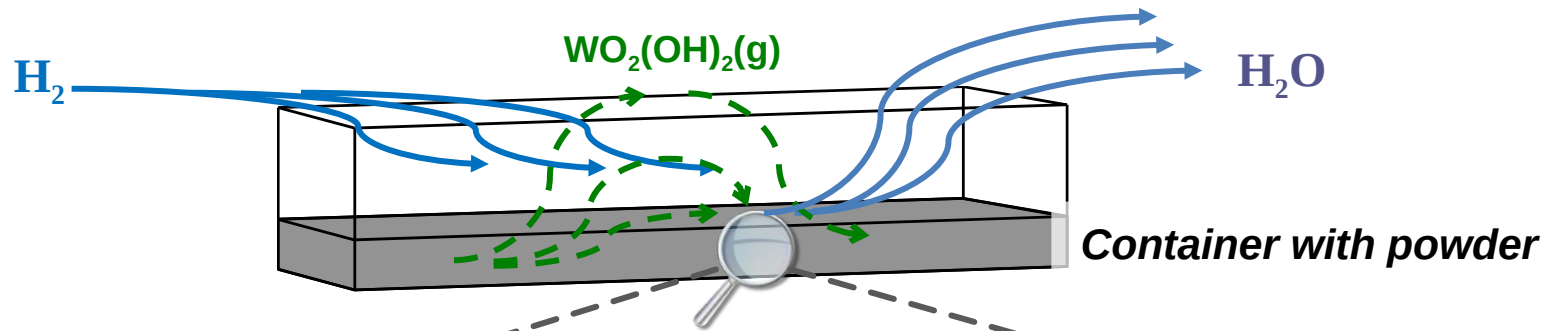
- A chemical optimization problem
- A grain growth proposed problem

☐ Takeaways

WHY?

Finding kinetic parameters for heterogeneous reaction systems

A chemical optimization problem



Finding kinetic parameters for heterogeneous reaction systems

A chemical optimization problem

SRC: Mónica Arenas, Maitsetseg Borchuluun, Léopold Hillah, 2020

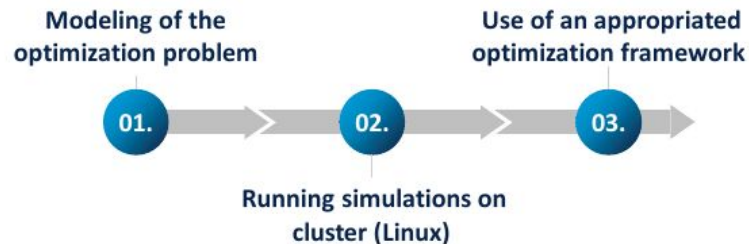


Introduction

One of the most important aspects of heterogeneous reactions is to understand and quantify the **evolution of the different transformations**. For instance, during metal-oxides reduction processes, it is of high importance to quantify the rate at which the pure metal is formed.

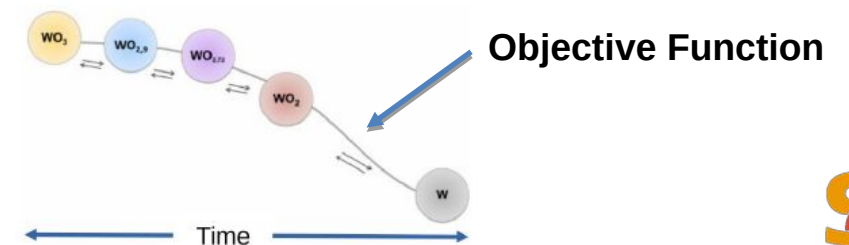
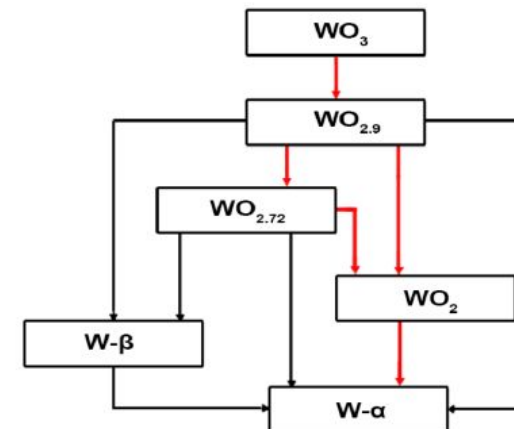
It is almost impossible to separately observe, accurately quantify and gain insight into these nonlinear physical and chemical processes by experimental means only. Thus, **XDEM** have become indispensable for studying complex systems without the need of costly experimental practices.

This tool is more efficient when implemented with optimization algorithms that help the finding of the **best optimal parameters**.



Goals

- Determine the **optimal parameters (E_a and k_r)** of each of the reduction steps involved in the dry-hydrogen reduction of tungsten trioxide.
- **Minimize the error** of XDEM simulations versus experimental data.



Why DAKOTA?

- One flexible simulation interface, a wide array of algorithms
- Advanced modeling and simulation, support for engineering transformation
- Scalable parallel computing from desktop to HPC

DAKOTA Calibration Approach



- Simulation-based Optimization
- Objective : Adjust model parameters x to maximize agreement with a set of experimental data

- Minimize

$$f(x) = \sum_{i=1}^n (s_i(x) - d_i)^2$$

simulation output that depends on x given data

- 3 Options:
 - Model returns simulation output to Dakota
 - Model returns residuals to Dakota
 - Model returns objective function value

Some methods:

- Tailored gradient-based
- Use any optimizer
- Bayesian inference



DAKOTA Optimization Approach

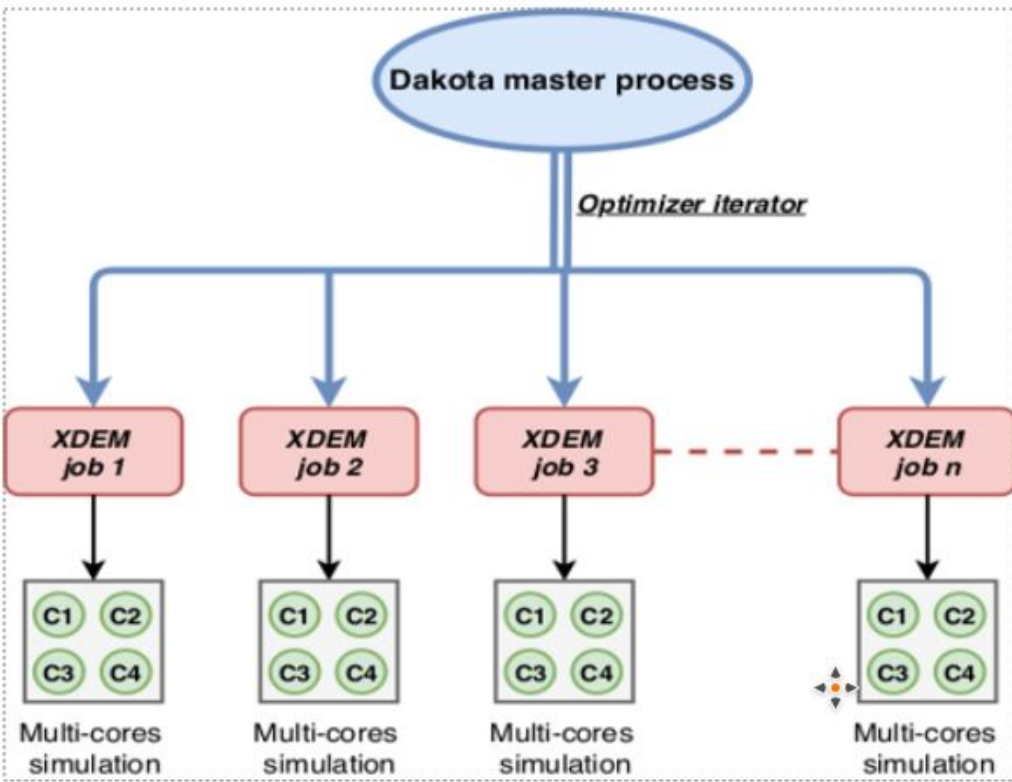
- Simulation-based Optimization
- Objective: Determine parameter values that yield extreme values (max/min) of objectives, while satisfying constraints
- Minimize / Maximize objective function
- 1 Option:
 - Model returns objective function value

Methods:

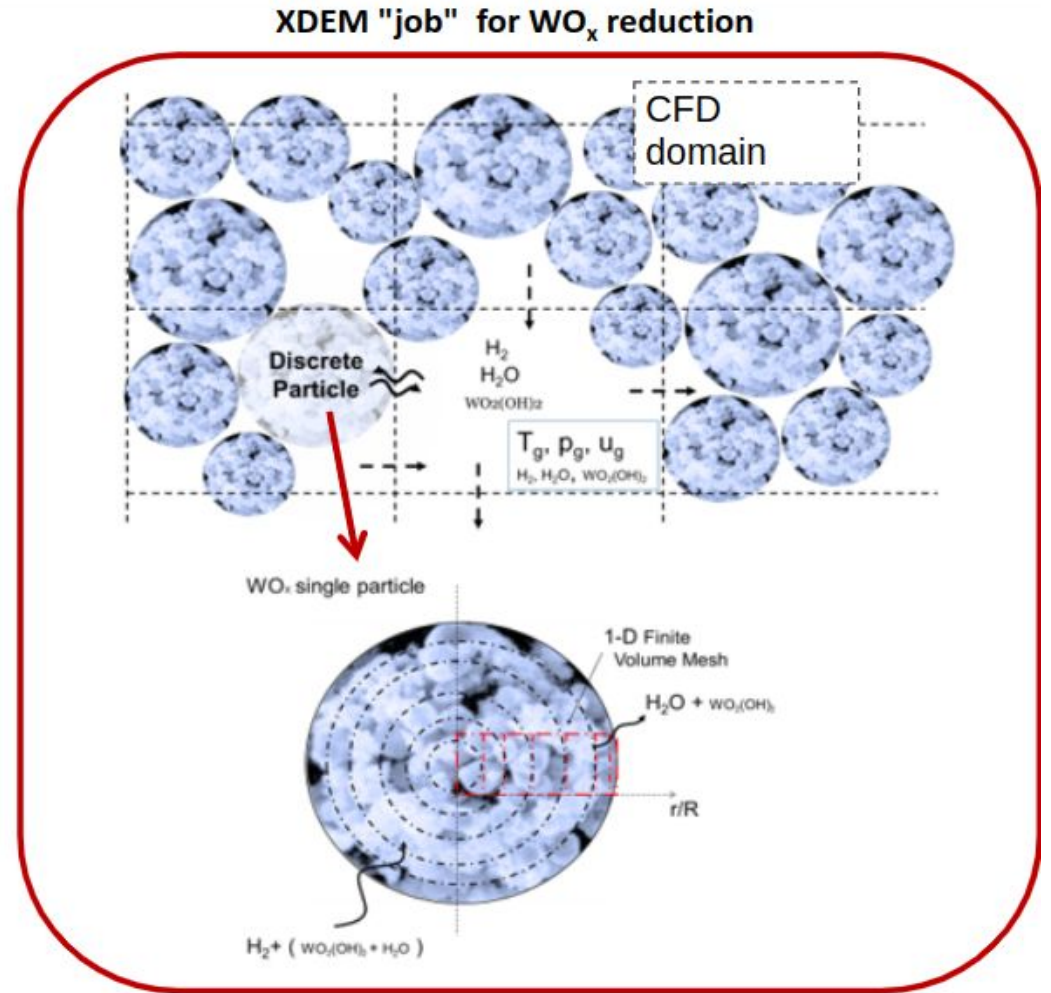
- Gradient-based local;
- Derivative-free local;
- Derivative-free global one can find Evolutionary Algorithms (EA), etc.;
- Global/heuristics
- Surrogate-based, multi-fidelity.

Any **Dakota optimization algorithm** can be applied to **calibration problems** arising in parameter estimation, system identification, and test/analysis reconciliation.

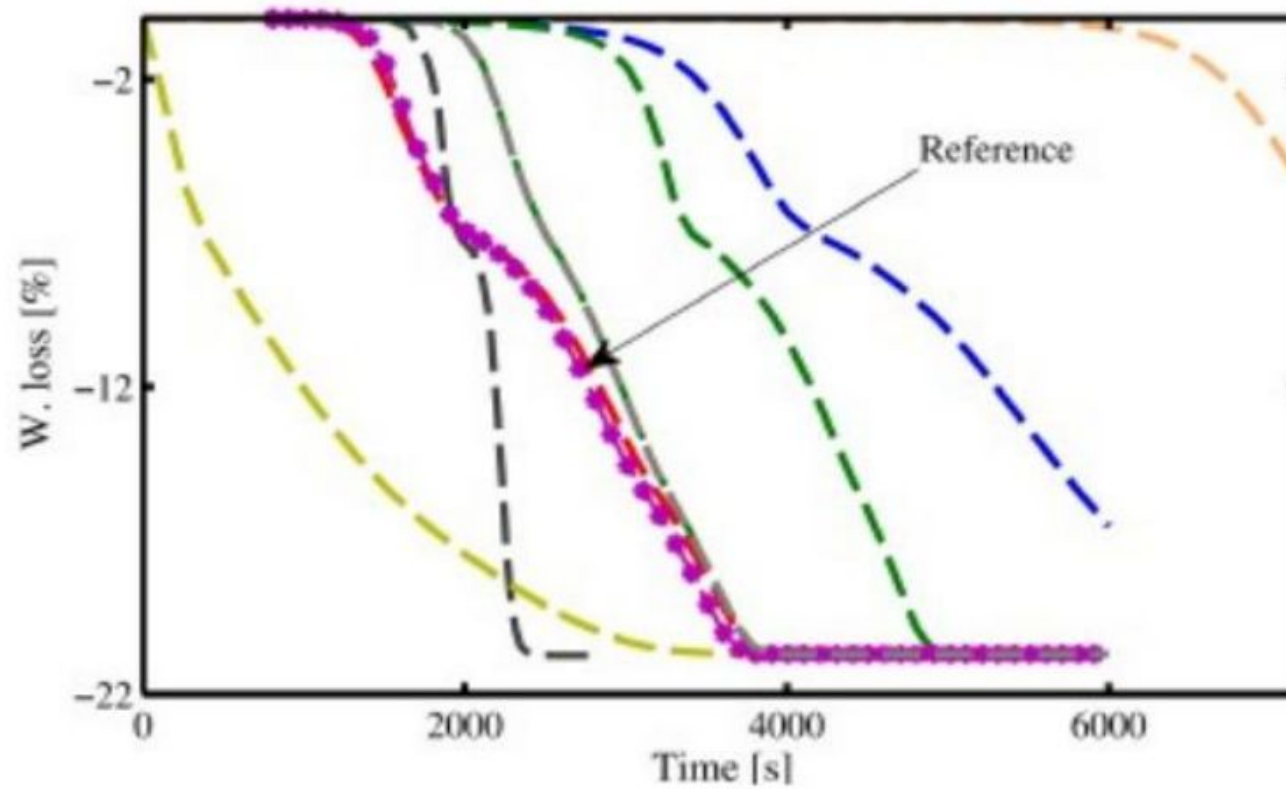
A chemical optimization problem



Source: Dr. A. Rousset, FNR grant *Grant 2018-2/13318107-VP4HPC*



A chemical optimization problem



Example of several "testing parameter" executions compared to the reference solution for the reduction of tungsten trioxide under dry atmospheres

A chemical optimization problem

SRC: Mónica Arenas, Maitsetseg Borchuluun, Léopold Hillah, 2020

- Hybrid approach
coliny_ea + optpp_newton

Impact of Variable Range Values on Convergence

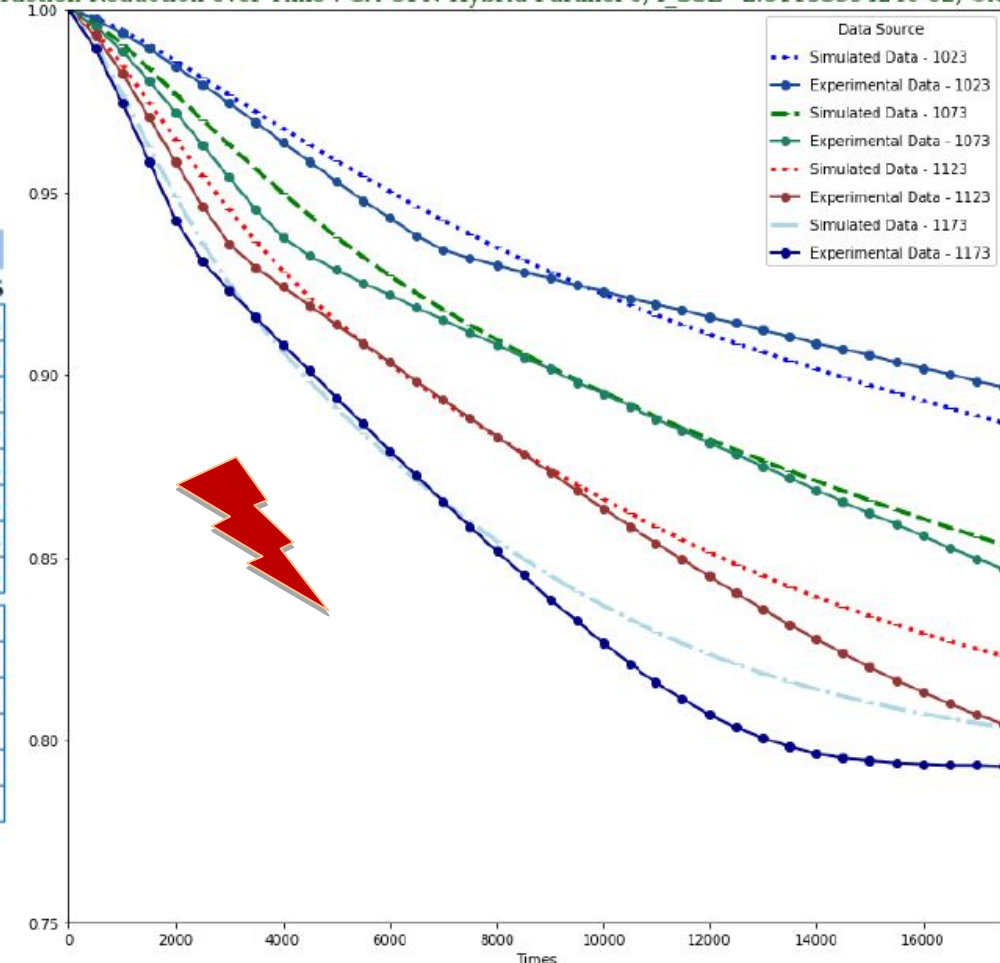
PARAMETERS	CASE 1		
	MIN	MAX	BEST PARAMETERS
ea1	1.00E-03	1.00E+06	1.74E+05
kr1	1.00E-03	1.00E+10	7.28E+09
ea2	1.00E-03	1.00E+06	8.47E+03
kr2	1.00E-03	1.00E+10	3.64E+09
ea3	1.00E-03	1.00E+06	1.68E+05
kr3	1.00E-03	1.00E+10	4.27E+09
ea4	1.00E-03	1.00E+06	6.30E+05
kr4	1.00E-03	1.00E+10	4.60E+09

Optimization Type	Hybrid Genetic Algorithm - Gauss Newton
Best Objective Function	1.92E-01
Function Evaluations	1071
XDEM Runs	4284
Total CPU (seconds)	3.94729
Total Wall Clock (seconds)	9579.55

PARAMETERS	CASE 2		
	MIN	MAX	BEST PARAMETERS
ea1	5.00E+04	1.00E+05	8.16E+04
kr1	1.50E+05	2.50E+05	1.68E+05
ea2	5.00E+04	1.00E+05	7.55E+04
kr2	3.00E+05	5.00E+05	3.69E+05
ea3	5.00E+04	1.00E+05	8.65E+04
kr3	3.00E+05	6.00E+05	3.23E+05
ea4	5.00E+04	1.00E+05	9.24E+04
kr4	9.00E+04	2.00E+05	1.68E+05

Optimization Type	Hybrid Genetic Algorithm - Gauss Newton
Best Objective Function	2.31E-02
Function Evaluations	1071
XDEM Runs	4284
Total CPU (seconds)	3.29619
Total Wall Clock (seconds)	13351.1

Mass Fraction Reduction over Time : GA-OPN Hybrid Parallel ϵ , $f_{SSE}=2.3115399424e-02$, Clock: 8212.48s



A chemical optimization problem

XDEM jobs: parallel performance

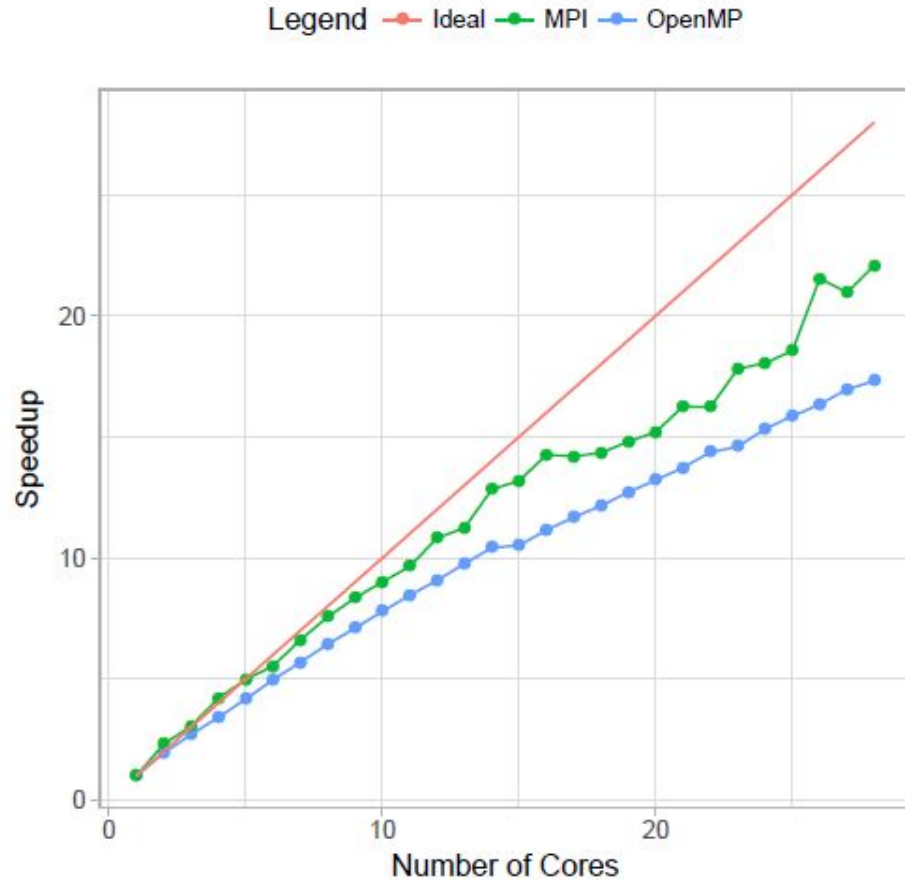


FIGURE 6.5: SpeedUp of MPI and OpenMP versions on one node i.e. up to 28 cores.

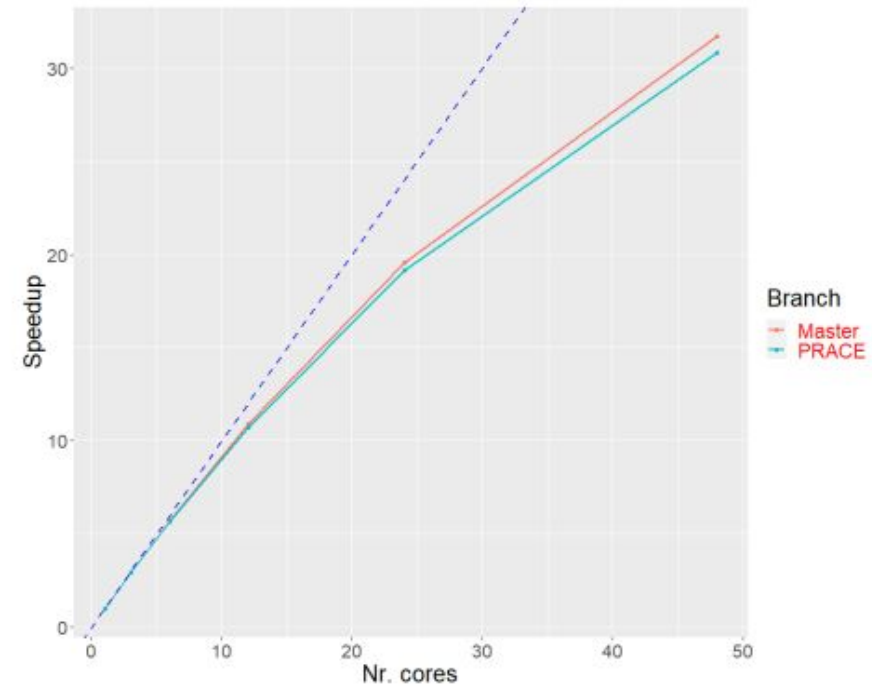
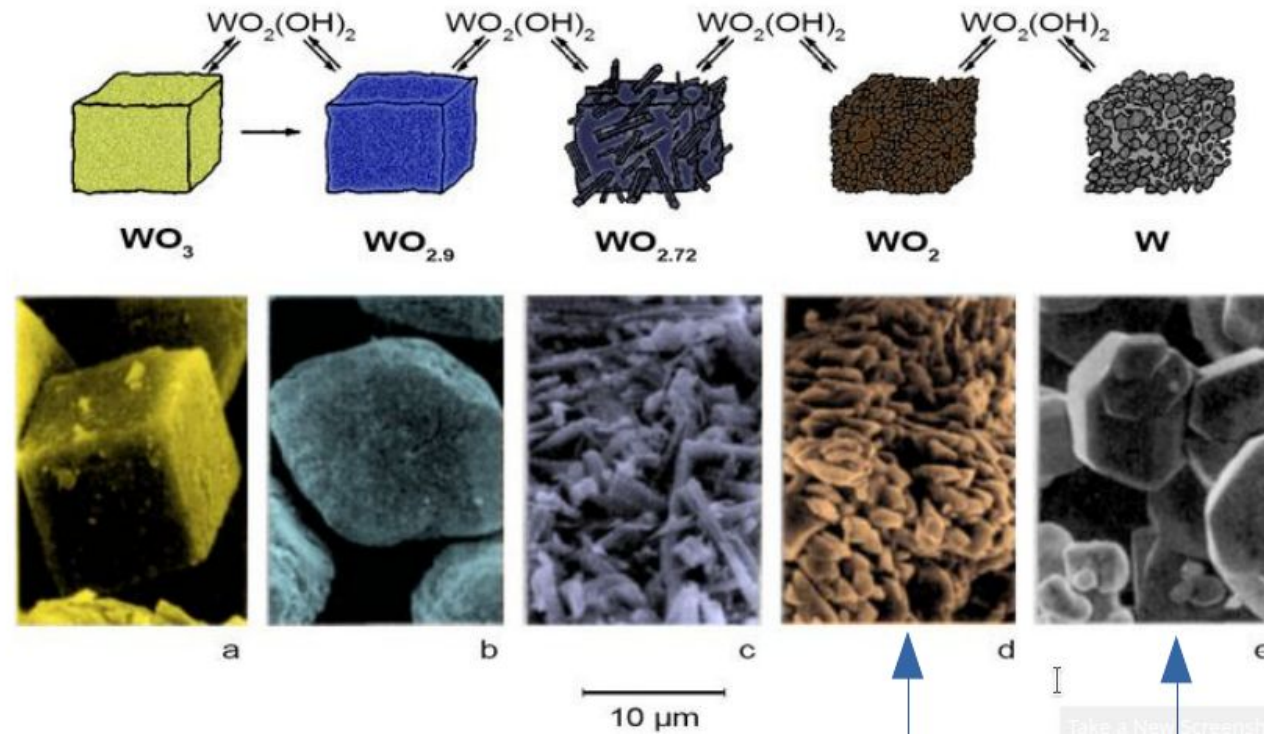
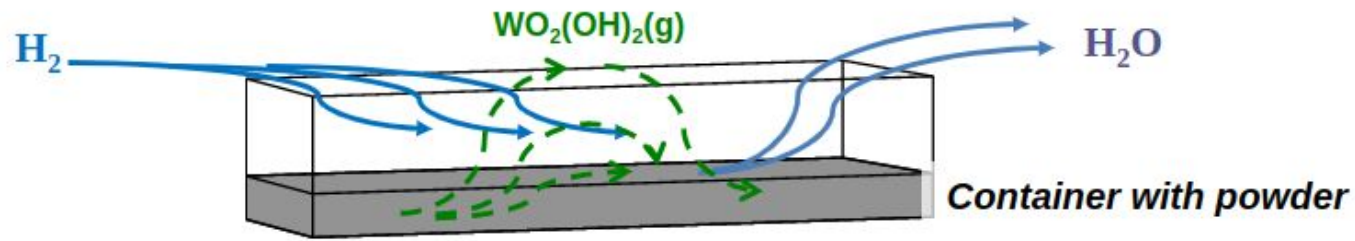


Figure 7. Speedup for the Conversion module as a function of the number of cores. Perfect scaling behaviour is shown with dashed-blue line.

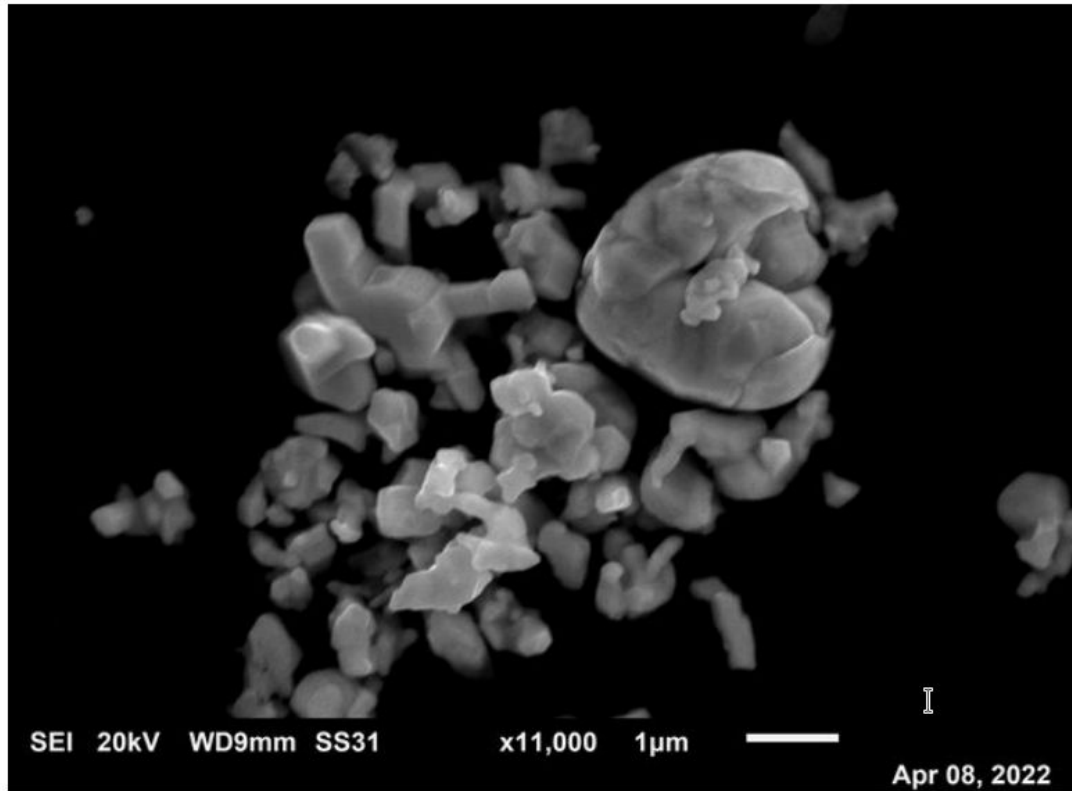
SRC: Mainassara Chekaraou, A.W., *Large Scale Parallel Simulation For Extended Discrete Element Method*, Doctoral Thesis, 2020

Rousset, A., *OpenMP optimisation of the eXtended Discrete Element Method (XDEM)*, Scientific Report, 2021

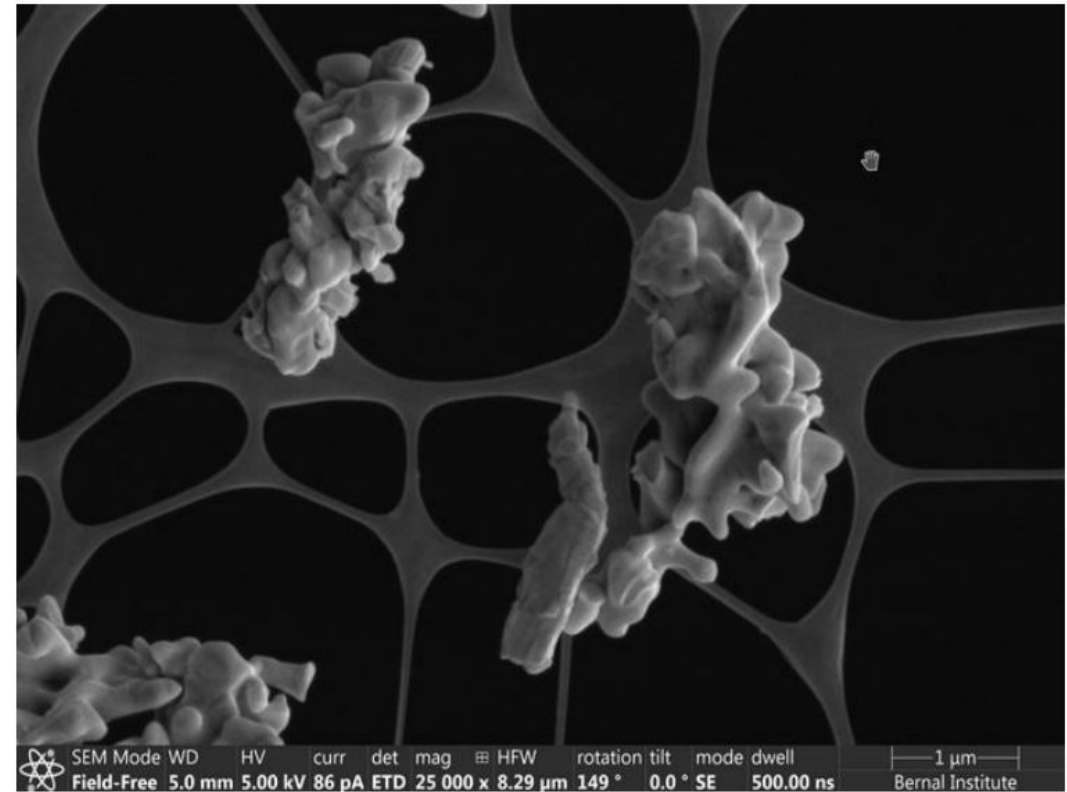
A grain growth proposed problem



A grain growth proposed problem



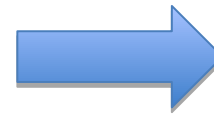
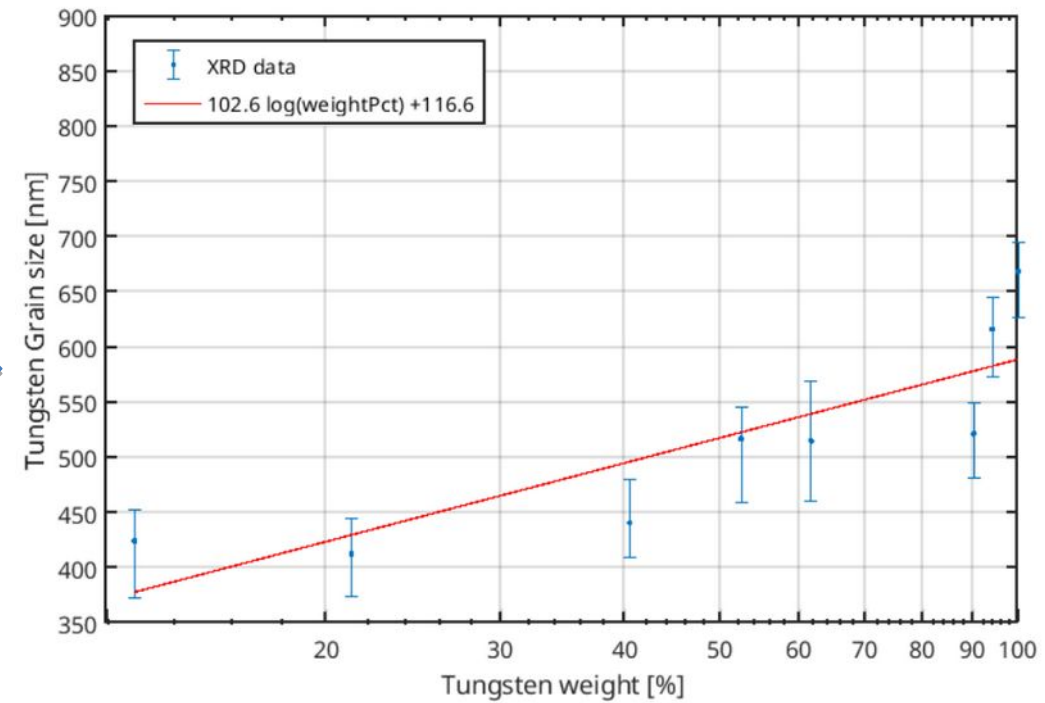
SEM image of WOx particles undergoing H2 reduction



TEM image of WOx particles undergoing H2 reduction

A grain growth proposed (optimization) problem

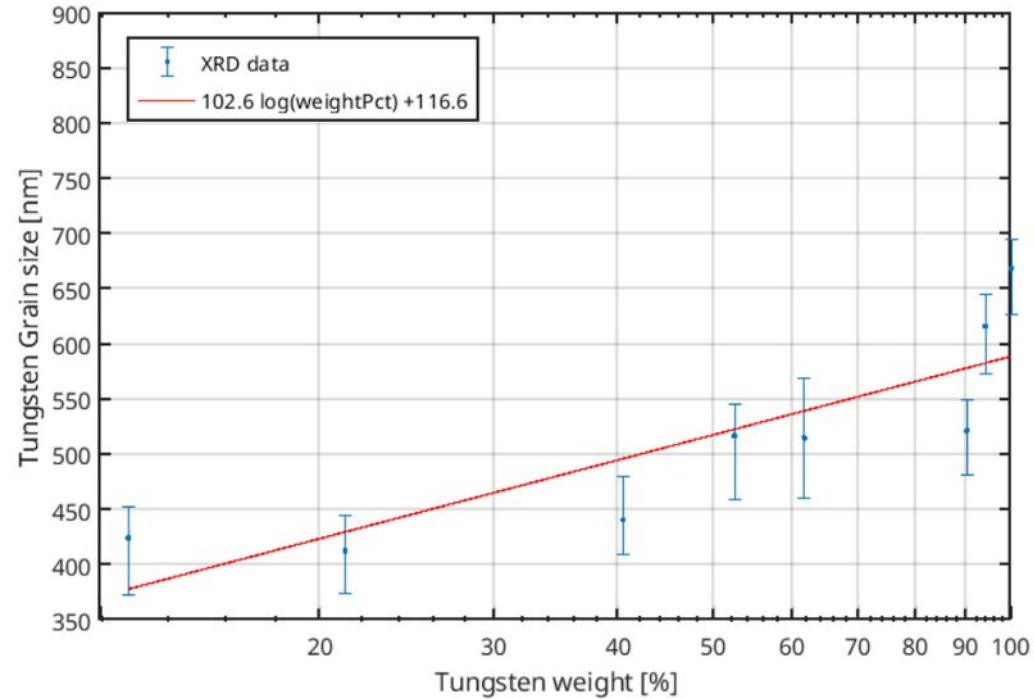
Objective Function



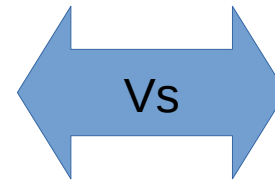
Synchrotron measurements: Volume reconstruction of Nano-holotomography.
Particle characteristic size $L = 25 \mu\text{m}$. ESRF (Grenoble-Fr).

A grain growth proposed (optimization) problem

Objective Function



XDEM simulations



Nucleation + grain growth parameters



Introduction

- Granular materials
- Reactions in heterogeneous particulate systems
- Numerical representations of reacting particulate systems
 - Lumped, continuous and discrete modeling approaches

Discrete Element Methods (DEM)

- DEM motivation and history
- Thermochemical DEM simulations
 - What simulation parameters are employed in thermochemical DEM simulations
 - A difference between large-scale and small-scale experimentation

Finding kinetic parameters for heterogeneous reaction systems

- A chemical optimization problem
- A grain growth proposed problem

Takeaways

- HPC has enabled an **accurate solution** of particulate systems undergoing physical/chemical transformations
 - Different modeling approaches for particulate systems
 - Extended discrete element methods are the closest numerical representation for particulate systems at "macro" scale
 - In a real world, particulate matter interacts with a continuous medium. This interaction it is of pivotal interest and needs to be accounted for
 - Warning: Reaction / diffusion parameters change with the dimension of the problem (except resolved methods)
 - Synergy between computer-sc, phyms and engineering for a successful large-scale simulation. *"Zapatero a sus zapatos"*
 - However, as a scientist, a good knowledge of both worlds is imperative for achieving meaningful results

Thank you!

- For more information on the University of Luxembourg: www.uni.lu
- For a virtual tour:
<https://luxdem.uni.lu>
<https://alvaro.estupinan.net>

Determination of Reaction Rate Parameters in Heterogeneous Particulate Systems

Dr. Alvaro A. ESTUPINAN DONOSO



UNIVERSITY OF LUXEMBOURG
Department of Physics
and Materials Science



Luxembourg National
Research Fund

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